Note

Gainers and the Losers: Real-time Industry PDs in the Covid-19 Crisis

1. Introduction

The Covid-19 crisis has generated a very particular and unprecedented pattern of credit quality changes across industry sectors. This pattern departs from that observed in past economic downturns. In a classic downturn, cyclically sensitive industries such as commercial property, investment goods, consumer durables producers, energy and materials exhibit clear credit deterioration. Banks may also experience financial distress if the downturn is severe.

In the Covid-19 crisis, firms involved in travel, bricks and mortar retail, hospitality, energy and financials have suffered significant deterioration. Companies engaged in health, a variety of technology sectors and internet retailers have actually performed better than they might have done in the absence of a crisis. Technology sectors have benefitted so markedly that this crisis is almost the inverse of the credit deterioration that followed the bursting of the technology bubble.

Tracking the evolution of credit quality across sectors is important for many financial institutions as they seek to adjust their risk management, pricing and limit setting. The crisis is likely to last many more months and understanding the cross-sectional impact will prove helpful for lenders navigating the resulting recession.

This note shows how representative probabilities of default (PDs) for individual industry sectors have evolved since the crisis began. The techniques applied permit one to refresh PD estimates in real time and, hence, offer extremely timely information about the state of corporate credit.

Our modelling approach uses sector equity and debt data to analyse the statistical behaviour of leverage ratios over time. Volatilities and higher moments of asset returns are used to infer probabilities of default which are then rescaled based on historical default probabilities.

The main findings are that the onset of the crisis in the first half of March 2020 boosted PDs for all sectors but that credit conditions in several 'gainer' sectors recovered quickly over the following month, leaving PDs lower than before the crisis. These gainers include Information Technology at the highest level of sector classification and, at the finest level for sector definitions: Health Care Technology, Internet and Direct Marketing Retail, Software, Technology Hardware, Storage and Peripherals, Biotechnology and Life Sciences Tools and Services. The falls in PDs for these latter fine categories range from 28% for Health Care Technology to 8% for Life Sciences.

For 'loser' sectors, PDs again rose sharply in March but have recovered only partially as the complexion of the crisis became somewhat clearer. 'Loser' sectors include most notably energy and financials among high-level sector categories. Among finer industry categories, a series of very specific sectors are major losers. These include Airlines (which experience a 50.56% increase in PDs since the start of 2020), Distributors (which see a 38.99% rise in PDs) and Hotels, Restaurants & Leisure (for which PDs rise by 32.76% since the start of the year)

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Overall, the change in PDs is not as major as many might expect given the level of disruption to economic activity worldwide. The asset values that feed into our estimates are signalling that the crisis is less serious than many might think at least as far as large corporate credit quality is concerned. This last conclusion is sensitive to the way in which we have projected forward corporate debt levels. As we obtain more information from company accounts following Q2 financial reports, we intend to refine the estimates.

The note is organised as follows. Section 2 briefly describes the methodology and data employed. Section 3 presents results for Global Industry Classification Standard¹ (GICS) sectors at Levels 1, 2 and 3. Section 4 concludes.

2. Methodology

Almost by definition, a company defaults when the total value of its assets (measured in a market rather than a book value sense) falls below the value of its debt. Statistical techniques permit one to infer the market value of a company's assets from its equity market capitalisation and its leverage. One can apply a similar logic to aggregate data from industries and thereby obtain representative leverage ratios and asset value volatilities.

Representative sector default probabilities may then be estimated using parametric models of the distribution of logarithm asset value changes. We employ both normal and t-distributions for this purpose. In the latter case, the additional degree of freedom parameter of the t-distribution may be inferred from the kurtosis of historical return series. We found that the t-distribution provides a more convincing description of the fat-tail feature of asset returns and, hence, we employ this distribution in our estimation of default probabilities.

Companies are classified into sectors based on Global Industry Classification Standard (GICS) definitions, which follows a hierarchical structure consisting of 11 sectors (Level 1), 24 industry groups (Level 2), 69 industries (Level 3) and 158 sub-industries (Level 4). To preserve adequate granularity while retaining reasonable numbers of individual companies in each category, we conduct our study based on Levels 1, 2 and 3. We rescale the PDs so that their levels at the beginning of 2020 are equivalent to the level of historical average PDs published in S&P (2019).

3. Results

3.1 GICS Level 1 Sector Results

Table 1 presents the PDs and other key statistics for GICS level 1 sectors. The third column shows percentage changes in MSCI sector indices between the start of 2020 and 11th June 2020. The Volatility column shows the standard deviations (or 'volatilities') of natural logarithm returns over half-year rolling windows for MSCI sector equity indices. The Leverage column is the D/E ratios from Bloomberg's company universe.

Table 1: Level 1 GICS Sector Probabilities of Default (PDs)

		Equity %							
		chg						PD % chg	PD % chg
GICS		1/1 to			PD start	PD	PD	1/1/20 to	since
code	Sector	11/6	Volatility	Leverage	2020	11/5/20	11/6/20	11/6/20	11/5/20
10	Energy	-35.53	24.12	61.29	3.05	4.80	4.70	54.13	-2.01
15	Materials	-10.77	28.10	35.14	2.48	3.01	2.79	12.31	-7.53
20	Industrials	-14.87	21.99	47.06	2.11	2.75	2.52	19.20	-8.45
25	Consumer Discretionary	-1.66	19.81	49.25	3.29	3.64	3.35	1.87	-7.85
30	Consumer Staple	-7.28	12.28	40.85	2.30	2.63	2.56	11.10	-2.91
35	Healthcare	-2.20	13.21	19.05	1.37	1.38	1.42	3.38	2.47
40	Financials	-24.00	27.75	53.85	0.66	0.91	0.85	28.38	-6.79
45	Information Tech	6.36	19.62	21.95	1.15	1.11	1.06	-7.88	-4.82
50	Telecom	-3.42	15.14	31.58	2.47	2.71	2.59	4.92	-4.27
55	Utilities	-8.50	14.60	66.67	0.43	0.51	0.48	10.79	-6.23
60	Real Estate	-15.13	24.31	69.49	0.69	0.83	0.80	15.50	-3.61
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Note: All the numbers are in percentages. Relative PD changes are measured in the last two columns. PD increases/decreases more than 10% are couloured dark red/green. PD increases/decreases between 5% and 10% are coloured light red/green.

¹ GICS was developed in 1999 by MSCI and Standard & Poor's.

Table 1 reveals that, leverage ratios vary dramatically across Level 1 GICS sectors. Real Estate, Utilities and Energy have the highest leverage ratios of 69.49%, 66.67% and 61.29%, respectively. Health Care has the lowest leverage of 19.05%, followed by Information Technologies (21.95%) and Telecom (31.58%). Equity markets also exhibit distinctly different performances. Despite an overall downward trend since the beginning of the year, Information Tech has outperformed its beginning of the year level by a remarkable 6.36%. Consumer Discretionary and Healthcare are only slightly affected by the crisis, with drops of 1.66% and 2.20%, respectively. Meanwhile, Energy and Financial sectors are hit hard by the crisis, suffering drops of 35.53% and 24%.

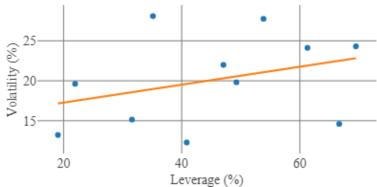
Figure 1 shows how PDs have evolved since the beginning of 2020 for GICS Level 1 sectors. Very different patterns may be observed across sectors. At the onset of the Covid-19 crisis in late February, PDs for all sectors start to increase, reaching a peak in mid-March. After that, Healthcare, Consumer Staple, Consumer Discretionary and Information Tech and Telecom sectors gradually recovered to pre-crisis levels. In contrast, for Energy, Industrials, Financials, Utilities and Real Estate, though some recovery is evident compared to peak crisis values, recovery has been slow.

Energy Materials PD (%) Mar 1 Jan 1 Jan 1 Mar 1 Industrials Consumer Discretionary © 3 € 2.5 PD (%) Healthcare Consumer Staple ş PD (%) 1.6 Jan 1 Feb 1 Mar 1 Jan 1 Feb 1 Mar 1 Apr 1 May 1 Information Tech Financials PD (%) € 0.9 0.8-0.7-Mar 1 Mar 1 Feb 1 May 1 Jan 1 Jan 1 Telecom Utilities PD (%) Apr 1 Real Estate All sectors PD (%) 0.8 0.7 Jan 1 Mar 1 Jan 1 Mar 1

Figure 1: PD since the Beginning of 2020 for GICS Level 1 Sectors

Figure 2 plots calibrated level 1 sector equity return volatilities against their current leverages. A line is fitted to the scatter points using Ordinary Linear Regressions. The upward sloping line shows the strong positive association between equity volatilities and leverages. The models employed in this note may be regarded as simple but consistent frameworks for differentiating the two primary influences on credit quality: leverage and volatility.

Figure 2: Scatter Plot of Level 1 Sector Leverage versus Volatility



Note: Leverage represents the debt to market capitalisation ratio. The line is fitted using Ordinary Linear Regression of all points.

3.2 GICS Level 2 Sector Results

Table 2 follows the same format as Table 1 in describing the PDs of more granular classifications. In most cases, subsectors within the same sector have the same directions in change in PDs. However, within Consumer Discretionary, Retailing subsector has become safer than its pre-crisis level, while Consumer Services, Consumer Durables & Apparel and Automobiles & Components have significantly increased PDs of 34.73%, 14.00% and 8.55%, respectively. The magnitude of the impact also differs across subsectors. This is most obvious for the Financials sector, within which the Diversified Financials subsector registers a 9.25% PD increase, while Banks and Insurance PDs increase by 39.31% and 35.57% respectively.

Table 2: Level 2 GICS Sector Probabilities of Default (PDs)

		Equity %					-		
		chg						PD % chg	PD % chg
GICS		1/1 to			PD start	PD	PD	1/1/20 to	since
code	Sector	11/6	Volatility	Leverage	2020	11/5/20	11/6/20	11/6/20	11/5/20
1010	Energy	-35.53	24.12	61.29	3.05	4.80	4.70	54.13	-2.02
1510	Materials	-10.77	28.10	35.14	2.48	3.01	2.79	12.31	-7.53
2010	Capital Goods	-17.21	24.00	47.06	3.63	4.86	4.42	21.71	-9.10
2020	Commercial & Professional Services	-5.45	16.67	36.99	0.70	0.81	0.75	7.57	-7.43
2030	Transportation	-12.44	17.79	63.93	2.00	2.46	2.31	15.55	-6.16
2510	Automobiles & Components	-8.32	24.40	56.25	5.93	7.12	6.44	8.55	-9.52
2520	Consumer Durables & Apparel	-11.92	22.09	53.85	3.78	4.77	4.31	14.00	-9.60
2530	Consumer Services	-21.53	18.13	44.93	1.19	1.69	1.60	34.73	-5.41
2540	Media	-0.21	20.73	49.25	3.07	3.18	3.08	0.22	-3.19
2550	Retailing	13.47	19.46	44.93	2.48	2.31	2.15	-13.28	-6.72
3010	Food & Staples Retailing	-4.24	12.35	44.93	2.53	2.71	2.68	6.05	-1.03
3020	Food, Beverage & Tobacco	-10.42	13.31	42.86	3.10	3.69	3.60	16.10	-2.23
3030	Household & Personal Products	-2.50	12.66	25.00	1.26	1.39	1.31	3.83	-5.84
3510	Health Care Equipment & Services	-4.76	16.74	23.46	2.36	2.46	2.52	7.07	2.40
3520	Pharmaceuticals, Biotechnology & Life Sciences	-0.66	12.75	16.28	0.38	0.38	0.39	1.01	2.42
4010	Banks	-31.15	29.38	53.85	0.53	0.80	0.73	39.31	-7.97
4020	Diversified Financials	-13.25	31.41	88.68	1.15	1.30	1.26	9.25	-3.36
4030	Insurance	-21.58	24.35	20.48	0.30	0.45	0.41	35.57	-9.42
4510	Software & Services	8.60	17.25	17.65	0.28	0.26	0.25	-11.01	-2.97
4520	Technology Hardware & Equipment	4.41	22.02	28.21	1.47	1.50	1.40	-5.12	-6.65
4530	Semiconductors & Semiconductor Equipment	3.38	24.61	21.95	1.69	1.74	1.63	-3.94	-6.48
5010	Telecommunication Services	-10.54	15.06	44.93	2.47	2.99	2.85	15.51	-4.42
5510	Utilities	-8.50	14.60	66.67	0.43	0.51	0.48	10.79	-6.23
6010	Real Estate	-15.13	24.31	69.49	0.69	0.83	0.80	15.50	-3.61
							-		

Note: All the numbers are in percentages. Relative PD changes are measured in the last two columns. PD increases/decreases more than 10% are couloured dark red/green. PD increases/decreases between 5% and 10% are coloured light red/green.

Figure 3 plots the time series of PDs for selected Level 2 sectors which have the largest increases or decreases in PDs. Semiconductors & Semiconductor Equipment and Technology Hardware Equipment have made quick recoveries after the crisis, probably because the demands for them have surged since the lockdown. Sectors of life essential goods normally have low elasticity on the demand side and are relatively stable. This is probably why Retailing has recovered quickly. Interestingly, also deemed as life essentials, Food, Beverages & Tobacco has a persistently higher PD than its previous level, which is possibly driven by its Beverages and Tobacco elements. Other more elastic consumer related sectors, such as Consumer Durables & Apparel and Consumer

Services, are still under the shadow of the crisis. As productions and trading activities drop, Energy and Capital Goods are still being heavily affected.

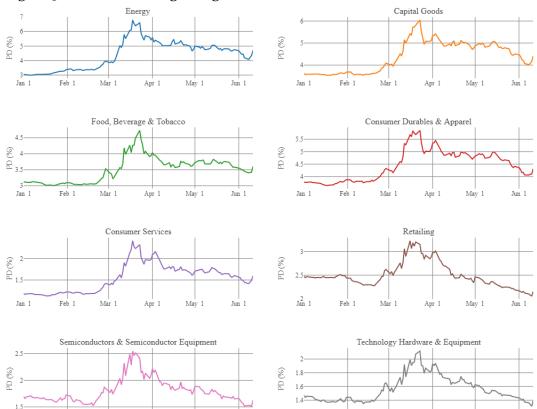
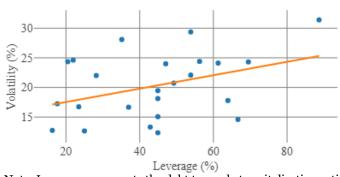


Figure 3: PD Since the Beginning of 2020 for Selected GICS Level 2 Sectors

The scatter plot of Level 2 (see Figure 4) shows wider ranges of leverage ratios and volatilities compared to Figure 1, indicating more diversities for sectors on a dis-aggregated level. Consistent with Figure 1, this plot has a similar upward trend line fitted to data points.



Apr 1

Figure 4: Scatter Plot of Level 2 Sector Leverage versus Volatility

Note: Leverage represents the debt to market capitalisation ratio. The line is fitted using Ordinary Linear Regression of all points.

GICS Level 3 Sector Results

3.3 GICS Level 3 Sector Results

This Section presents sector results at a more granular level and discover phenomenon which is submerged by aggressions in the previous sections. Table 3 shows results for selected Level 3 sectors, which have the largest increases or decreases in PDs.

Apart from sectors that are identified as having elevated risks in the Level 1 and Level 2 analysis, we also find other risky sectors. Airlines, having a very high leverage ratio of 127.27%, suffer a 50.56% increase in PD since the beginning of the year. Hotels, Restaurants & Leisure is also 32.76% more likely to go bankrupt. Distributors are also heavily affected by the crisis with a 38.99% rise in PDs, indicating disruptions to trade and supply chains. Sectors for which PDs have declined include those related to healthcare and internet technologies.

Table 3: Selected Level 3 GICS Sector Probabilities of Default (PDs)

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253010 Hotels, Restaurants & Leisure -21.59 19.29 49.25 1.20 1.67 1.59 32.76 -5.1 203050 Transportation Infrastructure -20.86 23.99 53.85 1.29 1.85 1.63 26.36 -12.0 151020 Construction Materials -22.46 28.79 51.52 2.73 3.81 3.43 25.65 -9.9 302010 Beverages -14.45 13.81 29.87 1.69 2.17 2.12 25.15 -2.1 302030 Tobacco -15.05 16.63 33.33 4.74 6.08 5.90 24.52 -3.0 254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers	255010	Distributors	-23.85	23.27	29.87	1.24	1.87	1.72	38.99	-8.08
203050 Transportation Infrastructure -20.86 23.99 53.85 1.29 1.85 1.63 26.36 -12.00 151020 Construction Materials -22.46 28.79 51.52 2.73 3.81 3.43 25.65 -9.9 302010 Beverages -14.45 13.81 29.87 1.69 2.17 2.12 25.15 -2.1 302030 Tobacco -15.05 16.63 33.33 4.74 6.08 5.90 24.52 -3.0 254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging <t< td=""><td>403010</td><td>Insurance</td><td>-21.57</td><td>24.35</td><td>20.48</td><td>0.30</td><td>0.45</td><td>0.41</td><td>35.56</td><td>-9.42</td></t<>	403010	Insurance	-21.57	24.35	20.48	0.30	0.45	0.41	35.56	-9.42
151020 Construction Materials -22.46 28.79 51.52 2.73 3.81 3.43 25.65 -9.9 302010 Beverages -14.45 13.81 29.87 1.69 2.17 2.12 25.15 -2.1 302030 Tobacco -15.05 16.63 33.33 4.74 6.08 5.90 24.52 -3.0 254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06	253010	Hotels, Restaurants & Leisure	-21.59	19.29	49.25	1.20	1.67	1.59	32.76	-5.15
302010 Beverages -14.45 13.81 29.87 1.69 2.17 2.12 25.15 -2.1 302030 Tobacco -15.05 16.63 33.33 4.74 6.08 5.90 24.52 -3.0 254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 </td <td>203050</td> <td>Transportation Infrastructure</td> <td>-20.86</td> <td>23.99</td> <td>53.85</td> <td>1.29</td> <td>1.85</td> <td>1.63</td> <td>26.36</td> <td>-12.08</td>	203050	Transportation Infrastructure	-20.86	23.99	53.85	1.29	1.85	1.63	26.36	-12.08
302030 Tobacco -15.05 16.63 33.33 4.74 6.08 5.90 24.52 -3.0 254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80	151020	Construction Materials	-22.46	28.79	51.52	2.73	3.81	3.43	25.65	-9.93
254010 Media -17.46 21.16 49.25 3.07 4.06 3.79 23.57 -6.4 402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage &	302010	Beverages	-14.45	13.81	29.87	1.69	2.17	2.12	25.15	-2.18
402020 Consumer Finance -30.13 34.24 96.08 1.27 1.68 1.56 23.19 -7.1 501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20	302030	Tobacco	-15.05	16.63	33.33	4.74	6.08	5.90	24.52	-3.03
501010 Diversified Telecommunication Services -14.35 14.82 44.93 1.14 1.46 1.40 22.45 -4.0 551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	254010	Media	-17.46	21.16	49.25	3.07	4.06	3.79	23.57	-6.49
551050 Independent Power and Renewable Electricity Producers -21.80 26.39 75.44 1.33 1.69 1.62 22.05 -4.4 151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	402020	Consumer Finance	-30.13	34.24	96.08	1.27	1.68	1.56	23.19	-7.15
151030 Containers & Packaging -16.60 21.75 56.25 1.17 1.46 1.41 20.68 -3.4 251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	501010	Diversified Telecommunication Services	-14.35	14.82	44.93	1.14	1.46	1.40	22.45	-4.00
251010 Auto Components -19.06 28.20 56.25 7.45 9.61 8.95 20.26 -6.7 352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	551050	Independent Power and Renewable Electricity Producers	-21.80	26.39	75.44	1.33	1.69	1.62	22.05	-4.48
352030 Life Sciences Tools & Services 6.25 20.98 12.36 0.84 0.80 0.78 -7.91 -2.8 352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	151030	Containers & Packaging	-16.60	21.75	56.25	1.17	1.46	1.41	20.68	-3.48
352010 Biotechnology 6.18 15.83 9.89 0.16 0.14 0.14 -8.32 4.7 452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	251010	Auto Components	-19.06	28.20	56.25	7.45	9.61	8.95	20.26	-6.79
452020 Technology Hardware, Storage & Peripherals 9.63 24.89 29.87 2.21 2.13 1.99 -9.77 -6.4 451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	352030	Life Sciences Tools & Services	6.25	20.98	12.36	0.84	0.80	0.78	-7.91	-2.81
451030 Software 13.68 17.23 13.64 0.24 0.20 0.20 -16.75 -1.5	352010	Biotechnology	6.18	15.83	9.89	0.16	0.14	0.14	-8.32	4.70
	452020	Technology Hardware, Storage & Peripherals	9.63	24.89	29.87	2.21	2.13	1.99	-9.77	-6.42
255020 Internet & Direct Marketing Retail 31.16 28.52 23.46 3.83 3.07 2.86 -25.16 -6.7	451030	Software	13.68	17.23	13.64	0.24	0.20	0.20	-16.75	-1.54
	255020	Internet & Direct Marketing Retail	31.16	28.52	23.46	3.83	3.07	2.86	-25.16	-6.73
351030 Health Care Technology 32.18 28.01 13.64 4.75 3.70 3.41 -28.24 -7.8	351030	Health Care Technology	32.18	28.01	13.64	4.75	3.70	3.41	-28.24	-7.83

Note: All the numbers are in percentages. Relative PD changes are measured in the last two columns. PD increases/decreases more than 10% are couloured dark red/green. PD increases/decreases between 5% and 10% are coloured light red/green.

Figure 5: PD Since the Beginning of 2020 for Selected GICS Level 3 Sectors

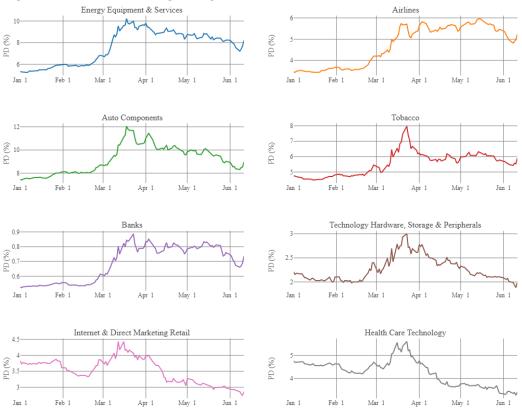
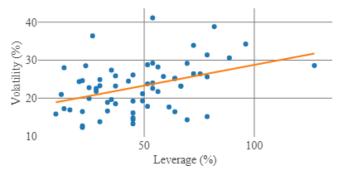


Figure 5 shows time series of selected Level 3 sectors. The sector having the most striking pattern is Airlines -its PD continues to rise after other sectors start to recover. Tobacco bounced back very quickly after the spike, compared to other sectors. Health Care Technology had the best performance among all sectors, with the ending PD being more than 1% less than its pre-crisis level.

The scatter plot shown in Figure 6 has a similar upward sloping line as in Figure 2 and Figure 4, although the ranges of volatilities and leverages are wider.

Figure 6: Scatter Plot of Level 3 Sector Leverage versus Volatility



Note: Leverage equals the debt to market capitalisation ratio. The line is fitted using Ordinary Linear Regression of all points.

4. Conclusions

This study analyses how PDs for different industries have evolved in the current Covid-19 crisis. We calculate daily PDs for GICS Level 1, 2 and 3 sectors from the start of 2020 until 11th June 2020 and analyse the variation across industry and time.

When the Covid-19 crisis deepened markedly in the first two weeks of March, PDs in all sectors rose dramatically. PD magnitudes increased proportionally by between 50% and 100% over a fortnight. After the initial spike, different sectors experienced quite diverse outcomes, partly reflecting the nature of the crisis and partly resulting from differences in representative leverage ratios and asset volatilities.

Among high-level industry sectors (GICS Level 1), the largest increases in credit risk occurred in Energy, Financials and Industrials sectors. Among sub-sectors (GICS Level 2), the worst affected were Energy, Banks, Insurers, and Consumer Services. Among finer sub-sectors (GICS Level 3), sectors that suffered most included Oil Gas & Consumable Fuels, Airlines, Banks and Automobile Components. Some sub-sectors not contained in the most affected Level 2 categories nevertheless suffered big PD increases. Such cases include Distributors, Tobacco and Hotels Restaurants & Leisure.

While all sectors saw increases in credit risk in the first half of March, some sectors, such as Healthcare and Information Technology made fast recoveries and by early June had lower PDs than before the crisis. Among GICS Level 2 sectors, the biggest gainers were Retailing and Software & Services, and Technology, Hardware & Equipment. From the Level 3 results, one may see that, in fact, the Retailers that benefitted were those using internet-based approaches. Overall, the strength of technology related sectors makes the credit impact of this crisis almost the inverse of the credit deterioration following the 2000-2002 bursting of the technology bubble.

Overall, the decline in PDs since their mid-March peak suggests that market data (on which our estimates are based) are consistent with a fairly rapid recovery in economic activity from the current turmoil. We intend to continue investigating the time paths of sectoral PDs over the next few months and to refine the approaches taken. In particular, we expect that as sectoral debt data comes available, it will be possible to discriminate further the credit impacts on different sectors.

Note that this note is part of a broad research program in which we are engaged to understand the impact of the crisis on credit markets. Other lines of research include (i) the derivation of conditional ratings for corporate credit portfolios, differentiating between sector, country and firm size, and (ii) the analysis of PDs and ratings for banks worldwide.

Appendix 1: GICS Level 3 PDs

Table A1: Level 3 GICS Sector Probabilities of Default (PDs)

		Equity %							
		chg						PD % chg	PD % chg
		1/1 to			PD start	PD	PD	1/1/20 to	since
GICS code	Sector	11/6	Volatility	Leverage		11/5/20	11/6/20	11/6/20	11/5/20
101010	Energy Equipment & Services	-50.75	38.81	81.82	5.31	8.48	8.21	54.68	-3.20
101020	Oil, Gas & Consumable Fuels	-34.64	22.59	53.85	0.79	1.28	1.25	57.75	-2.04
151010	Chemicals	-10.15	23.19	36.99	1.03	1.26	1.16	12.85	-7.90
151020	Construction Materials	-22.46	28.79	51.52	2.73	3.81	3.43	25.65	-9.93
151030	Containers & Packaging	-16.60	21.75	56.25	1.17	1.46	1.41	20.68	-3.48
151040	Metals & Mining	-7.71	36.39	26.58	3.66	4.25	3.93	7.54	-7.53
151050	Paper & Forest Products	-19.65	29.17	69.49	3.82	4.63	4.52	18.41	-2.43
201010	Aerospace & Defense	-28.29	21.82	28.21	0.83	1.46	1.27	52.27	-13.14
201020	Building Products	-10.62	26.11	44.93	3.78	4.74	4.22	11.72	-11.02
201030	Construction & Engineering	-16.57	25.14	63.93	4.36	5.55	5.12	17.58	-7.69
201040 201050	Electrical Equipment Industrial Conglomerates	-10.97 -18.66	25.86 25.62	36.99 78.57	2.97 5.45	3.73 6.83	3.35 6.43	13.11 18.08	-10.12 -5.86
201030	Machinery	-10.47	27.37	35.14	3.43	4.27	3.89	12.14	-8.81
201000	Trading Companies & Distributors	-10.47	25.71	58.73	4.56	5.36	5.12	12.14	-4.44
202010	Commercial Services & Supplies	-7.50	16.13	44.93	0.70	0.82	0.77	10.31	-5.89
203010	Air Freight & Logistics	-8.93	19.24	44.93	0.70	0.63	0.57	11.60	-9.81
203010	Airlines	-47.39	28.58	127.27	3.47	5.72	5.23	50.56	-8.63
203020	Marine	-20.15	31.37	78.57	4.33	5.41	5.05	16.57	-6.69
203040	Road & Rail	-8.63	16.43	63.93	0.40	0.46	0.44	10.62	-3.40
203050	Transportation Infrastructure	-20.86	23.99	53.85	1.29	1.85	1.63	26.36	-12.08
251010	Auto Components	-19.06	28.20	56.25	7.45	9.61	8.95	20.26	-6.79
251020	Automobiles	-4.77	23.75	51.52	4.42	5.19	4.64	4.95	-10.61
252010	Household Durables	-9.04	24.48	42.86	4.58	5.52	5.05	10.40	-8.45
252020	Leisure Products	-9.15	18.90	33.33	1.19	1.55	1.34	13.01	-13.52
252030	Textiles, Apparel & Luxury Goods	-13.55	23.19	66.67	5.57	7.00	6.37	14.36	-9.00
253010	Hotels, Restaurants & Leisure	-21.59	19.29	49.25	1.20	1.67	1.59	32.76	-5.15
253020	Diversified Consumer Services	1.80	19.64	35.14	1.18	1.04	1.15	-2.15	10.61
254010	Media	-17.46	21.16	49.25	3.07	4.06	3.79	23.57	-6.49
255010	Distributors	-23.85	23.27	29.87	1.24	1.87	1.72	38.99	-8.08
255020	Internet & Direct Marketing Retail	31.16	28.52	23.46	3.83	3.07	2.86	-25.16	-6.73
255030	Multiline Retail	-7.62	23.14	66.67	3.63	4.11	3.90	7.48	-5.07
255040	Specialty Retail	-2.78	17.68	61.29	1.24	1.36	1.28	3.12	-5.82
302010	Beverages	-14.45	13.81	29.87	1.69	2.17	2.12	25.15	-2.18
302020	Food Products	-4.36	13.26	44.93	2.88	3.12	3.06	6.12	-2.03
302030	Tobacco	-15.05	16.63	33.33	4.74	6.08	5.90	24.52	-3.03
303010	Household Products	-1.20	12.31	21.95	0.21	0.21	0.21	1.83	-2.66
303020	Personal Products	-4.59	19.91	25.00	2.32	2.74	2.47	6.35	-9.77
351010	Health Care Equipment & Supplies	-4.49	16.92	16.28	0.42	0.43	0.45	6.80	4.18
351020	Health Care Providers & Services	-7.04	18.54	36.99	1.90	2.06	2.08	9.57	0.92
351030	Health Care Technology	32.18	28.01	13.64	4.75	3.70	3.41	-28.24	-7.83
352010	Biotechnology	6.18	15.83	9.89	0.16	0.14	0.14	-8.32	4.70
352020	Pharmaceuticals	-3.31	12.72	21.95	0.15	0.15	0.16	5.17	2.18
352030	Life Sciences Tools & Services	6.25	20.98	12.36	0.84	0.80	0.78	-7.91	-2.81
401010	Banks	-31.15	29.22	53.85	0.53	0.80	0.73	39.51	-8.01
401020	Thrifts & Mortgage Finance	20.24	41.12	53.85	4.40	4.00	4.00	10.15	2.72
402010	Diversified Financial Services	-20.24	33.89	72.41	1.12	1.33	1.30	16.15	-2.72
402020	Consumer Finance	-30.13	34.24	96.08	1.27	1.68	1.56	23.19	-7.15
402030 403010	Capital Markets Insurance	-7.75 -21.57	30.60	88.68	1.08	1.17 0.45	1.13 0.41	5.18 35.56	-3.09 -9.42
451020	IT Services	2.13	24.35 16.48	20.48 21.95	0.30 0.33	0.43	0.41	-2.93	-4.89
451020	Software	13.68	17.23	13.64	0.33	0.33	0.20	-16.75	-1.54
452010	Communications Equipment	-6.12	22.76	25.00	1.04	1.16	1.13	8.14	-2.69
452020	Technology Hardware, Storage & Peripherals	9.63	24.89	29.87	2.21	2.13	1.13	-9.77	-6.42
452030	Electronic Equipment, Instruments & Components	-5.91	22.54	28.21	1.17	1.37	1.26	7.69	-8.29
453010	Semiconductors & Semiconductor Equipment	3.37	24.61	21.95	1.69	1.74	1.63	-3.94	-6.48
501010	Diversified Telecommunication Services	-14.35	14.82	44.93	1.14	1.46	1.40	22.45	-4.00
501010	Wireless Telecommunication Services	0.89	17.85	51.52	3.80	3.96	3.76	-1.01	-5.07
551010	Electric Utilities	-6.56	14.32	69.49	0.13	0.15	0.14	8.04	-7.04
551020	Gas Utilities	-10.70	14.38	44.93	0.07	0.09	0.09	16.02	-2.42
551030	Multi-Utilities	-11.09	15.16	78.57	0.19	0.22	0.21	13.42	-4.99
551050	Independent Power and Renewable Electricity Producers	-21.80	26.39	75.44	1.33	1.69	1.62	22.05	-4.48
601010	Equity Real Estate Investment Trusts (REITs)	-15.07	25.23	63.93	0.61	0.73	0.70	15.62	-3.94
601020	Real Estate Management & Development	-16.72	26.42	72.41	0.77	0.92	0.90	16.05	-2.44
		1			7.17		-	Di	

Note: All the numbers are in percentages. Relative PD changes are measured in the last two columns. PD increases/decreases more than 10% are couloured dark red/green. PD increases/decreases between 5% and 10% are coloured light red/green.

Appendix 2: Detailed Methodology and Data Description

PD calculation methodology

This section provides a non-technical description of the methodology employed in estimating sector probabilities of default (PDs). Corporate finance models of the firm suggest that the ratio of forward-looking estimates of firm asset values to debt is the key driver of default.

Let D/E denote the debt equity ratio of a representative firm at a given moment in time. Assume that debt D remains constant within a year and the market value of equity is denoted E. Total assets equal A = D + E. Suppose that changes in the logarithm of asset values over a 1-year period are Gaussian with mean μ and volatility σ_A .

$$\Delta \ln (A) \sim N(\mu, \sigma_A) \tag{A2.1}$$

Here, $\ln(\cdot)$ is the natural logarithm function, and $N(\cdot)$ indicates the normal distribution. Assume $\mu = 0$. Let t equal the current time and t+1 is a year from now. The one-year default probability is

$$PD = P\left(\frac{A_{t+1}}{D} < 1\right) = P\left(\ln\left(\frac{A_{t+1}}{A_t}\right) < \ln\left(\frac{D}{A_t}\right)\right) = \Phi\left(\frac{\ln\left(\frac{D}{A_t}\right) - \mu}{\sigma_A}\right)$$
(A2.2)

 $\Phi(\cdot)$ is the cumulative distribution function of the normal distribution.

The volatility of assets is hard to estimate directly but one may easily obtain equity return volatilities. Assume the number of shares is constant so that the volatility of total equity market capitalisation equals the volatility of equity prices (denoted σ_E). Asset volatility σ_A can be inferred from σ_E . Define E = A - D and f(E) = (E + D)/D. From this, one may derive the approximate relation:

$$\frac{df}{f} = \frac{E}{E+D} \times \frac{dE}{E}$$
 so $\sigma_A \cong \sigma_E \times \frac{E}{E+D}$ (A2.3)

Suppose that log equity changes for individual firms have a single common factor denoted X. For a given firm (with index i) the change in log equity may be expressed as:

$$\Delta \ln(A_i) = \sigma_A \times \left(\sqrt{\rho} X + \sqrt{1 - \rho} \varepsilon_i\right) \tag{A2.4}$$

Here, *X* and ε_i are independent random variables with unit variances and zero means.

A fully diversified equity index representing investments in individual firms will not be exposed to risk associated with the ε_l firm-level shocks. Hence, individual firm volatilities σ_E will be related to the index volatility denoted σ_l through the equation:

$$\sigma_E = \sigma_I / \sqrt{\rho} \tag{A2.5}$$

Using the above results, we wish to infer representative probabilities of default (PDs) for firms in a given sector.

If we identify the common factor, $\sigma_I X$, with the (suitably de-meaned) log change in a sector index, to calculate the default probability in equation (2), we must calibrate three parameters: σ_I , ρ and the leverage ratio D/E.

Note that the above approach presumes that the random factor driving asset values is Gaussian. When the approach is implemented for firms that have low leverage, default probabilities may be implausibly small because the assumption of Gaussianity makes the likelihood of large changes in asset value extremely small. An alternative approach is to suppose that the random factor driving default has a fat-tailed distribution such as that of a Student's t-distributed random variable.

If we replace the assumption in equation (1) with:

$$\Delta \ln (A) \sim T(\mu, \sigma_A, \nu) \tag{A2.6}$$

Here, v denotes the degrees of freedom parameter of the t distribution. Then, the same sequence of steps may be followed except that the Gaussian cumulative distribution function $\Phi(.)$ in equation (2) is replaced with T(.|v).

Rescaling

All Level 1 GICS sectors and two GICS Level 2 sectors are one-to-one mapped to sectors in the Standard & Poor's report². For a given sector, supposed the PD calculated by the model on 1st January 2020 is P^B , and the PD from the S&P report is $P^{S\&P}$. The whole series of a given sector is scaled by multipling $P^{S\&P}/P^B$. The mapping is shown in Table 1.

Table A2.1: Mapping of Sectors in S&P Report to GICS

			S&P's weighted average PD
Sectors in S&P's report	GICS sector	GICS code	(%, 1981 - 2018)
Aerospace/auto/capitalgoods/metals	Industrials	20	2.11
Consumer/service	Consumer staple	30	2.3
Energy & natural resources	Energy	10	3.05
Financial institutions	Financials	40	0.66
Forest & building products/homebuilders	Materials	15	2.48
Health care/chemicals	Healthcare	35	1.37
High tech/computers/officeequipment	Information tech	45	1.15
Leisure time/media	Consumer discretionary	25	3.29
Real estate	Real estate	60	0.69
Telecommunications	Telecom	50	2.47
Utility	Utilities	55	0.43
Insurance	Insurance	4030	0.3
Transportation	Transportation	2030	2

Suppose that a Level 1 sector contains a set of N Level 2 sub-sectors. We rescale the PDs of these sub-sectors so that their average equals the PD of their parent sector.

The before-scaling and after-scaling Level 1 PDs are denoted P^B and P^A . Let the corresponding PDs for the ith sub-sector before and after scaling be denoted P_i^B and P_i^A . In the case when none of the sub-sectors has been rescaled already, we rescale the sub-sector PDs using the equation:

$$P_i^A = P_i^B \times \frac{P^A}{\sum_i P_i^B / N} \tag{A2.7}$$

Suppose that we already observe pre- and post-scaling PDs for one Level 2 sector with subscript j. Then for each sub-sector i for $i \neq j$, given a set of unscaled PDs, P_i^B , we can deduce the scaled PDs P_i^A for i = 1, 2, ..., N for $i \neq j$ using the following equation:

$$P_i^A = P_i^B \times \frac{P^A - P_j^A/N}{\sum_{i \neq j} P_i^B/N}$$
 (A2.8)

Given a set of before and after scaling PDs for Level 2, P_i^B and P_i^A for i=1,2,...,N, we can infer the after scaling PDs for Level 3 sectors using the formula where $P_{k,i}^B$ and $P_{k,i}^A$, respectively denote the PDs before and after scaling for a Level 3 sub-sector k within a Level 2 sub-sector k, for k=1,2,...K.

$$P_{k,i}^{A} = P_{k,i}^{B} \times \frac{P_{i}^{A}}{\sum_{k} P_{k}^{B} / K}$$
 (A2.9)

Data

We use the Global Industry Classification Standard (GICS) developed by MSCI and S&P Dow Jones to define sectors. The GICS approach is widely used in studies of firm financial performance and valuation. It has a hierarchical structure consisting of 11 sectors (Level 1), 24 industry groups (Level 2), 69 industries (Level 3) and 158 sub-industries (Level 4). To preserve adequate granularity while retaining reasonable numbers of individual companies in each category, we conduct our study based on Levels 1, 2 and 3.

The mean sectoral leverage is calculated from all active public companies in the Bloomberg universe, under its EQS function. The universe contains 90,963 companies, of which 45,439 have GICS sector data. Leverage ratios are calculated for each company as total debt divided by the sum of total debt, preferred stock and the market

² See Standard & Poor's (2019)

value of common stocks, as of the current date. The provided aggregation functionality of EQS enable us to group the companies by its GIC sectors, industry groups and industries, and derive the average of leverage ratios. These ratios are then transformed to the D/E ratio required. Where there are too few companies (fewer than 5) in a certain category, the average leverage obtained as described above may not be reliable. In this case, the leverage ratio of the parent category is employed (instead of using the average of companies within the category).

MSCI sector indices track the daily price performance of equities for a certain sector. The indices are based on the GICS sector taxonomy. The sector indices are downloaded for Levels 1, 2 and 3 GICS sectors. A sample period from the middle of 2006 to 11th June 2020 is employed in the volatility estimation. Note that according the volatility of an index is smaller than the volatilities of individual companies due to the elimination of company-specific risks. We, therefore, adjust the index volatilities for idiosyncratic risk equation (5). In this adjustment ρ is set to 0.18. This is the mid-point of the range of factor weights employed in the Basel II risk weight formula, namely 12% to 24%.

Last, if the above approach is implemented using a t distribution rather than assuming that risk factors are Gaussian, one must calibrate the degrees of freedom parameter, v. For this purpose, we calculated the average kurtosis of sector index returns. As it holds for t-distributions that $kurtosis - 3 = \frac{6}{v-4}$, (v > 4), we infer that v = 5.5.